Neural Guided Program Synthesis

AAAI’22 & **JOSS’22**

with N.Fijalkow, G.Lagarde, T.Matricon, K.Ellis, P.Ohlmann, A.Potta

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Program Synthesis?

An old dream: Church's Problem (1957)

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Logical formulas

Specification = ϕ a logical formula
A program **P** such that for all x, $\phi(x, P(x)) = True$

Natural language

« A program that removes odd elements and sort the rest »

A set of I/O examples

```
[1, 5, 4, 2]  ⟶  [2, 4]
[6, 3, 0, 8]  ⟶  [0, 6, 8]
```

Today's setting! aka « *Inductive Program Synthesis* »

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SORT; FILTER(EVEN)

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Similarities with machine learning

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Program Synthesis	Machine learning
Small number of examples	Large amount of data
Combinatorial/Symbolic search	Optimisation
Satisfies all specifications (reliable)	Minimizes a loss function (noisy)
Program (interpretable)	Model (hard to understand)

DeepCoder

Microsoft (Balog et al., 2017) — it manipulates list of integers

Program 4:

```
x ← [int]
y ← [int]
c ← SORT x
d ← SORT y
e ← REVERSE d
f ← ZIPWITH (*) d e
g ← SUM f
```

Input-output example:

Input:

```
[7 3 8 2 5],
[2 8 9 1 3]
```

Output:

```
79
```

Description:
Xavier and Yasmine are laying sticks to form non-overlapping rectangles on the ground. They both have fixed sets of pairs of sticks of certain lengths (represented as arrays `x` and `y` of numbers). Xavier only lays sticks parallel to the x axis, and Yasmine lays sticks only parallel to y axis. Compute the area their rectangles will cover at least.

TF-Coder

Google (Shi et al. 2019) — it manipulates tensors in Tensorflow

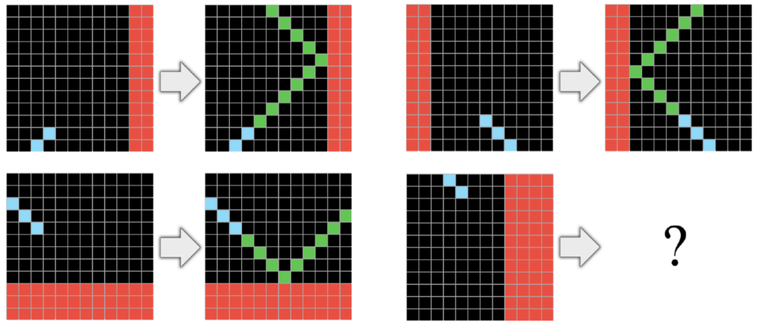
```
# Input-output example
inputs = {
    'scores': [[0.7, 0.2, 0.1],
               [0.4, 0.5, 0.1],
               [0.4, 0.4, 0.2],
               [0.3, 0.4, 0.3],
               [0.0, 0.0, 1.0]],
}
output = [[1, 0, 0],
          [0, 1, 0],
          [1, 0, 0],
          [0, 1, 0],
          [0, 0, 1]]
```

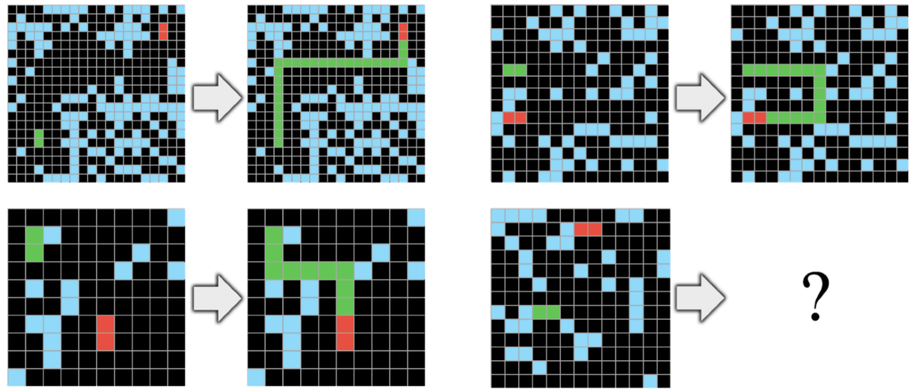
TF-Coder uses a combination of `tf.one_hot` and `tf.argmax` in a short solution to this problem:

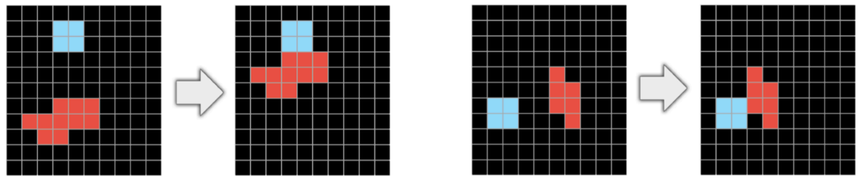
```
tf.cast(tf.one_hot(tf.argmax(scores, axis=1), 3), tf.int32)
```

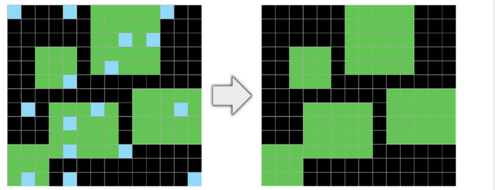
ARC Dataset

« The Abstraction and Reasoning Corpus », in « On the measure of intelligence » François Chollet, 2019







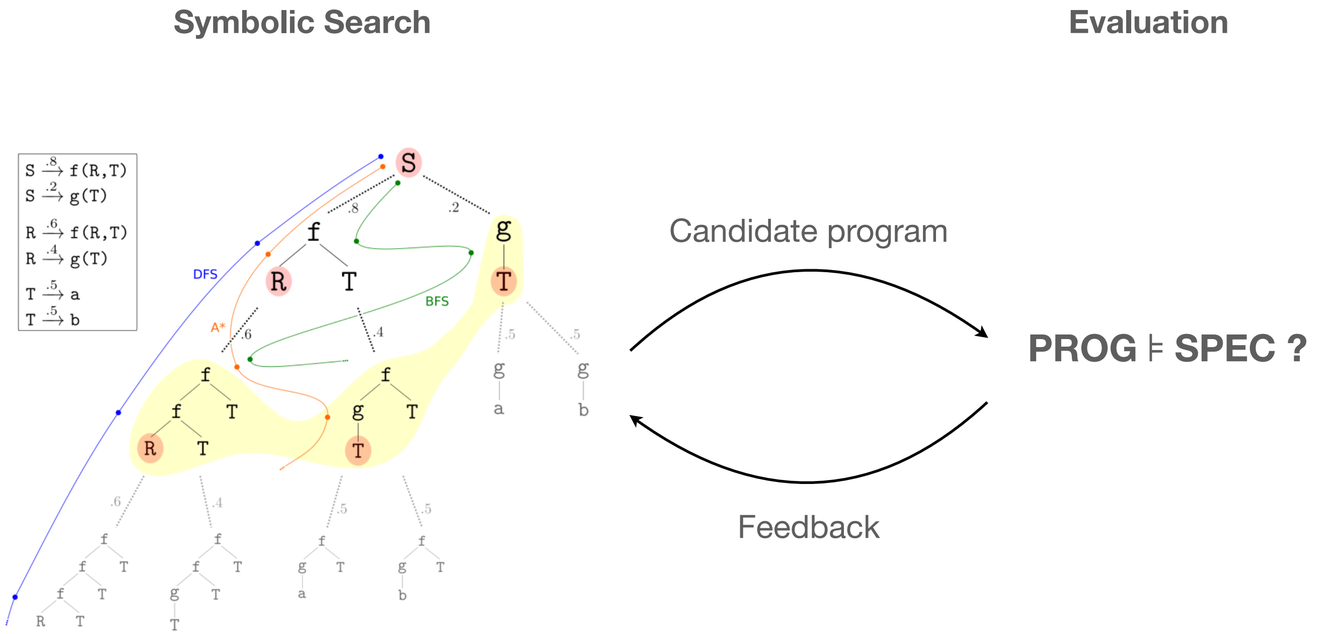


Neural-Guided Program Synthesis

Combination of formal methods and machine learning

reliable

efficient



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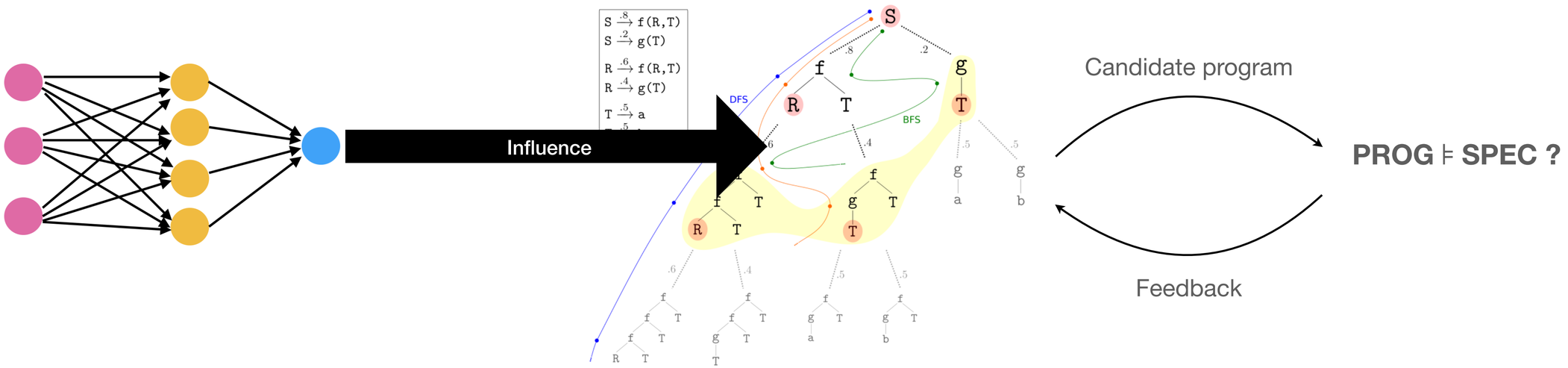
Machine Learning Predictions

Symbolic Search

Evaluation



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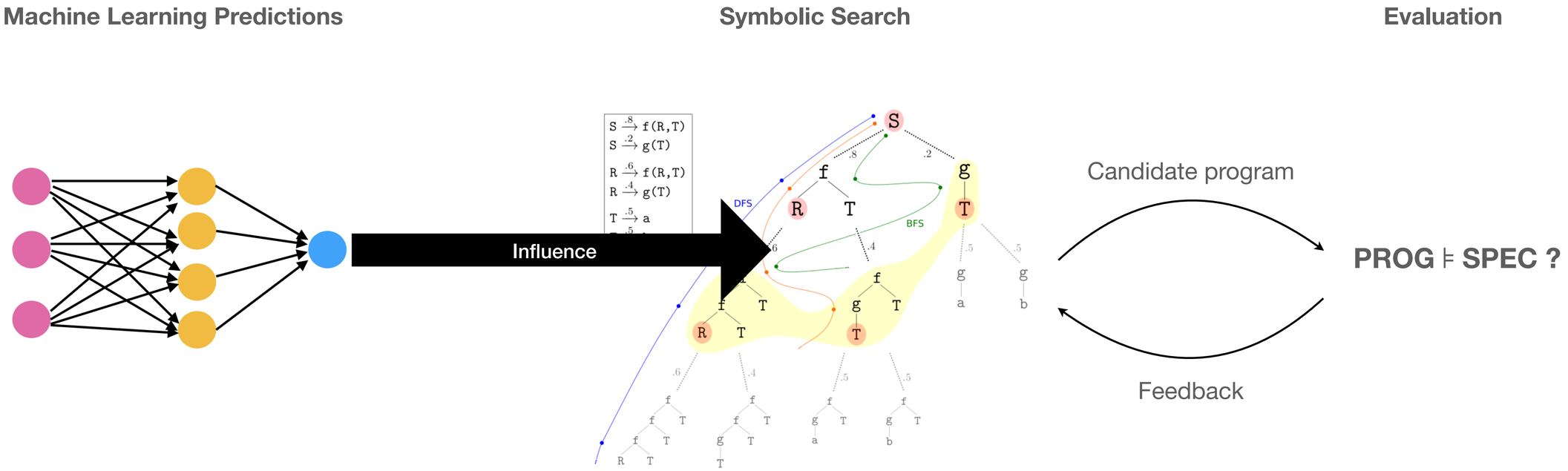
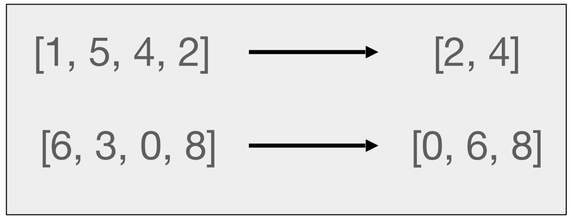


First practical instance: DeepCoder, 2017

Natural idea: patterns found in examples reveal which primitives are used in a solution program



Likely primitives such that:

- SORT
- FILTER[EVEN]
- MULTIPLY[2]
- …

Program representation

DSL: domain specific language
- Designed for a specific class of tasks
- List of primitives + associated types + semantics

DSL

```
sort : list(int) → list(int)
car : list(t) → t
cdr : list(t) → list(t)
map : (t1 → t2) →
        list(t1) → list(t2)
range : int → list(int)
+ : int → int → int
1 : int
        ⋮
```

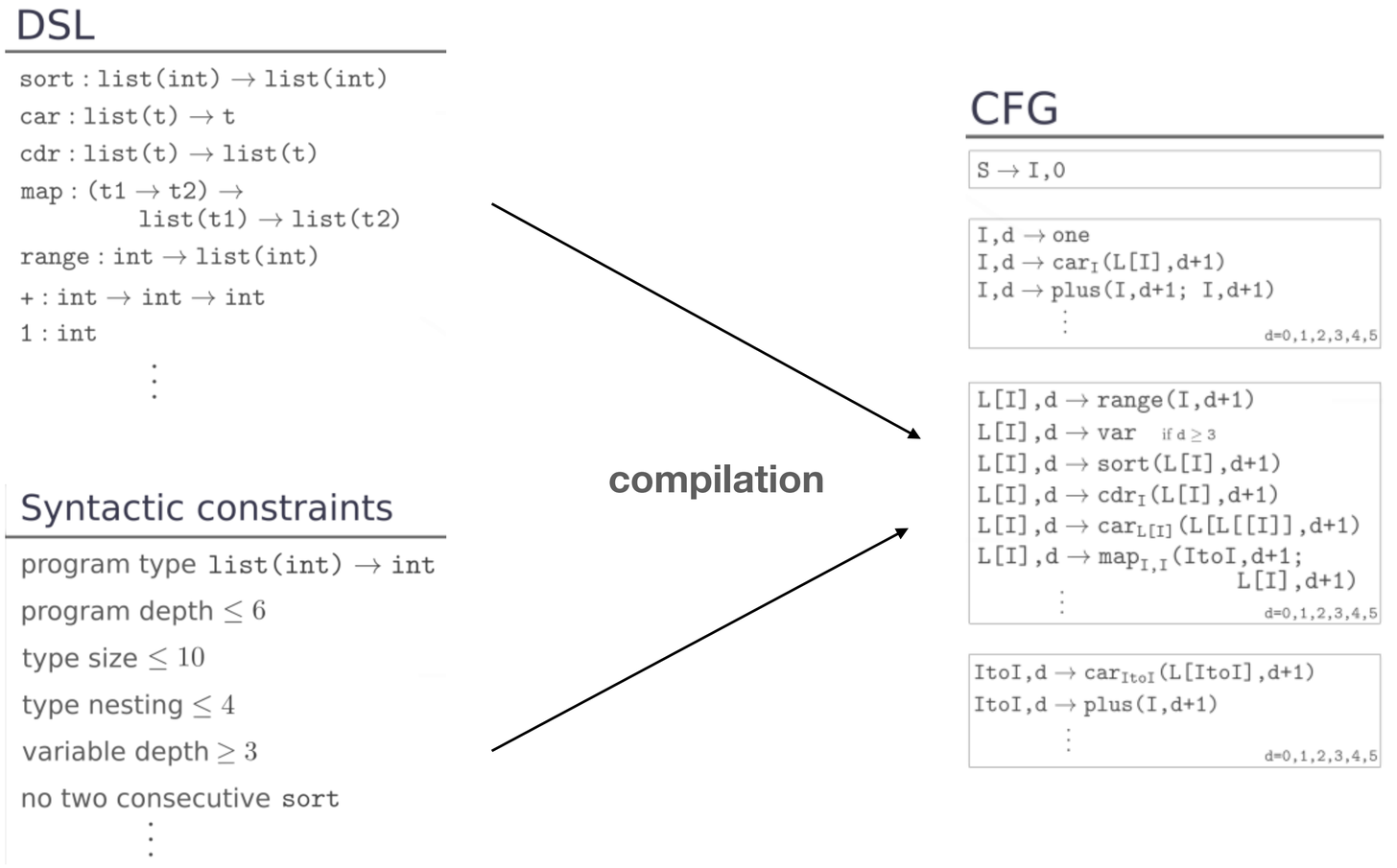
SyGUS in its own words

The Problem

A Syntax-Guided Synthesis problem (SyGuS, in short) is specified with respect to a background theory $\mathbb{T}$, such as Linear-Integer-Arithmetic (LIA), that fixes the types of variables, operations on types, and their interpretation.

To synthesize a function f of a given type, the input consists of two constraints:
(1) a *semantic constraint* given as a formula φ built from symbols in theory $\mathbb{T}$ along with f, and **(2)** a *syntactic constraint* given as a (possibly infinite) set $\mathcal{E}$ of expressions from $\mathbb{T}$ specified by a context-free grammar.
The computational problem then is to find an implementation for the function f, *i.e.* an expression $e \in \mathcal{E}$ such that the formula $\varphi[f \leftarrow e]$ is valid.

DSL —> Context-free Grammar



From CFG to PCFG

CFG

$$S \rightarrow \quad f(S,S) \;+\; g(T)$$

$$T \rightarrow \quad a \;+\; b$$

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$$T \rightarrow \quad a \; + \quad b$$

PCFG

$$S \rightarrow \frac{1}{4} \cdot f(S,S) \; + \frac{3}{4} \cdot g(T)$$

$$T \rightarrow \frac{2}{3} \cdot a \; + \frac{1}{3} \cdot b$$

From CFG to PCFG

A PCFG *induces* a distribution D over **trees = programs**

CFG

$$S \to f(S,S) + g(T)$$
$$T \to a + b$$

PCFG

$$S \to \frac{1}{4} \cdot f(S,S) + \frac{3}{4} \cdot g(T)$$
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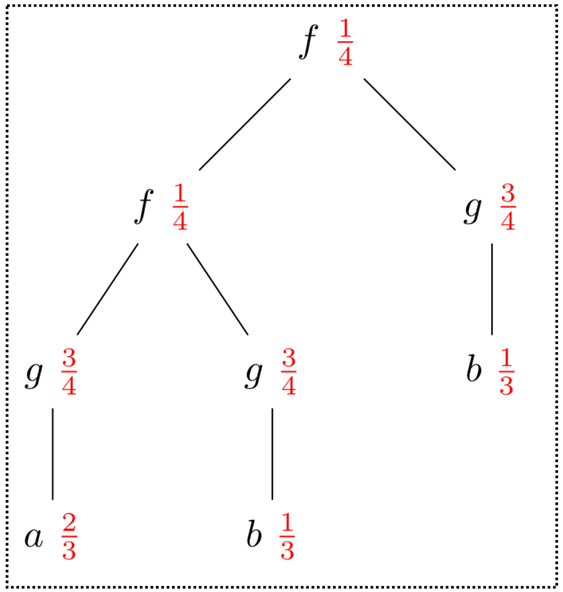

Probability = $\frac{1}{4} \cdot \frac{1}{4} \cdot \frac{3}{4} \cdot \frac{2}{3} \cdots$

Predictions: learning the PCFG

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$Pr(SORT \mid REV)$ is low

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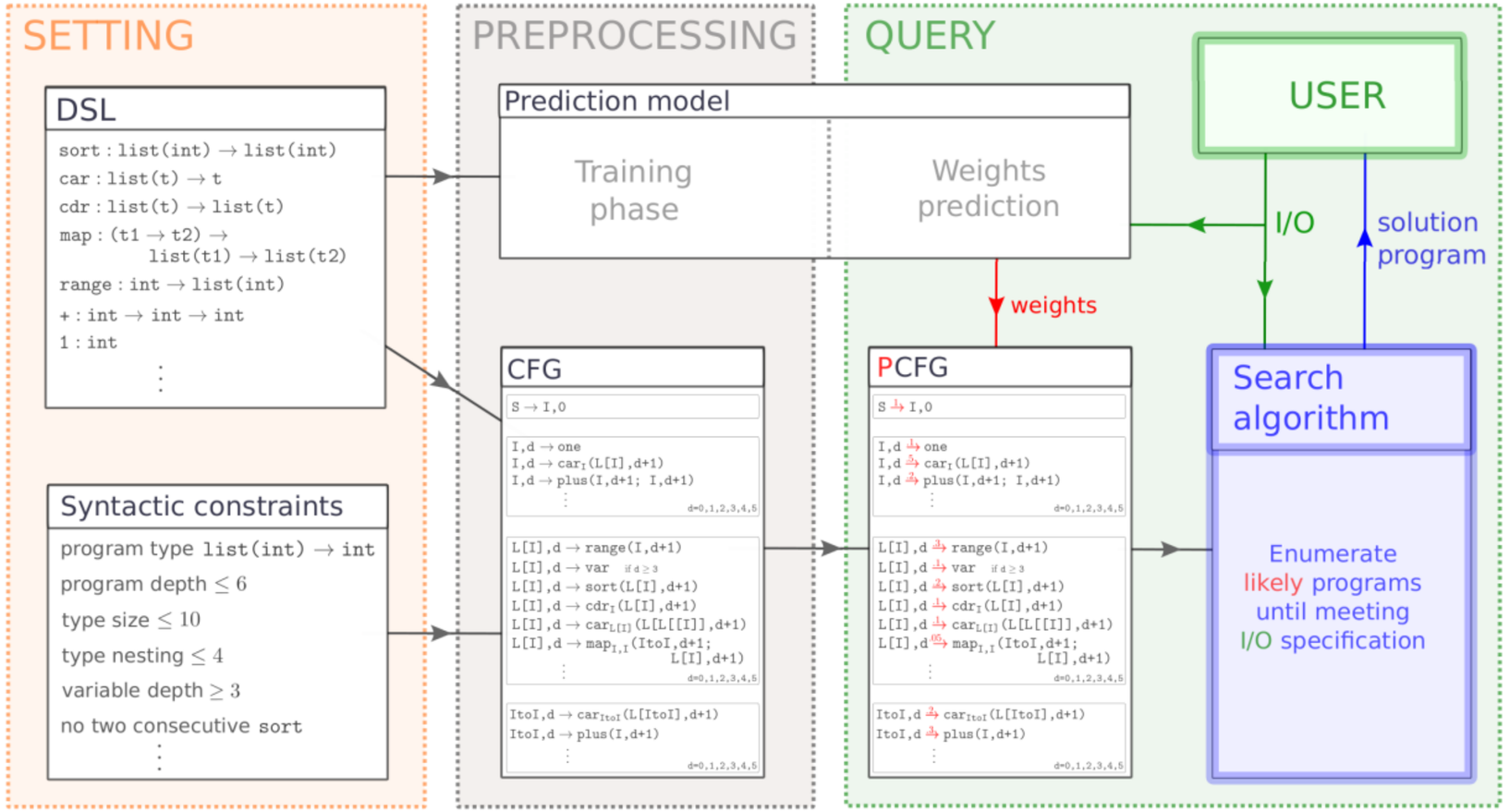
The prediction model induces a **prior** distribution $D = Pr(program \mid examples)$

Summary so far



We are here!

How to use predictions for the search?

Toy example on the board

Technical contributions

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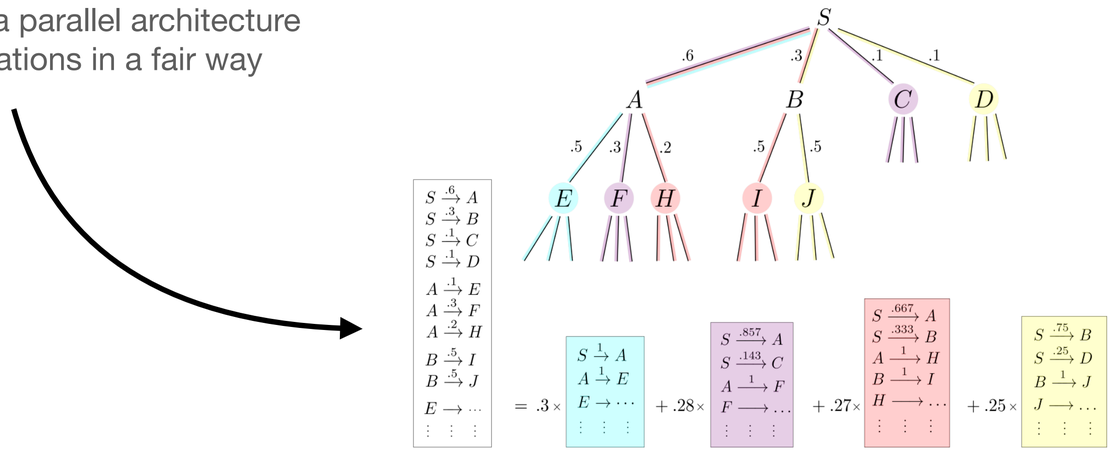
Heap Search.
Bottom-up enumeration strategy preserving the order on programs

- **Idea**: collections of heaps for storing partial programs
- **Guarantee**: i-th program in time $O(\log i)$

Grammar Splitting.
Divide the search on a parallel architecture

- **Idea**: partition derivations in a fair way



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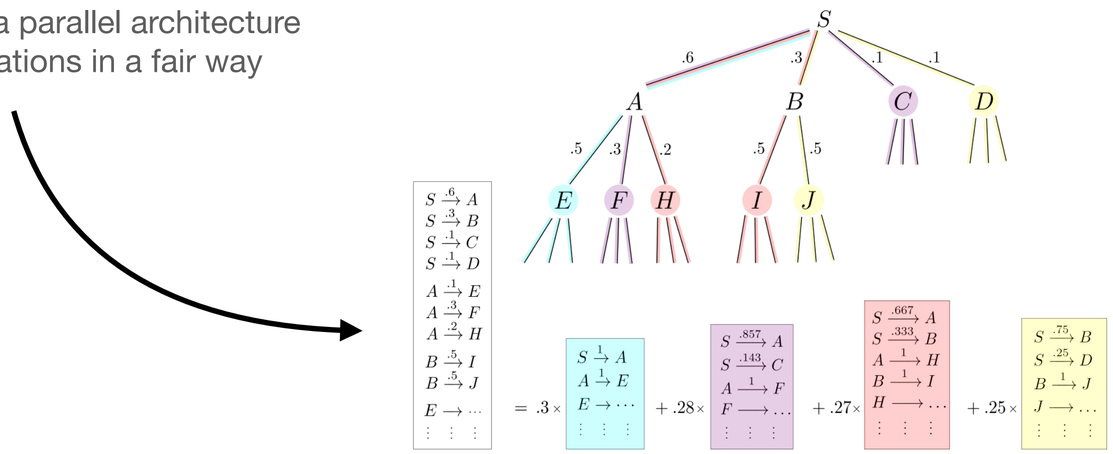

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SQRT Sampling.
Optimal sampling strategy with no memory
Interesting for simplicity and parallel search
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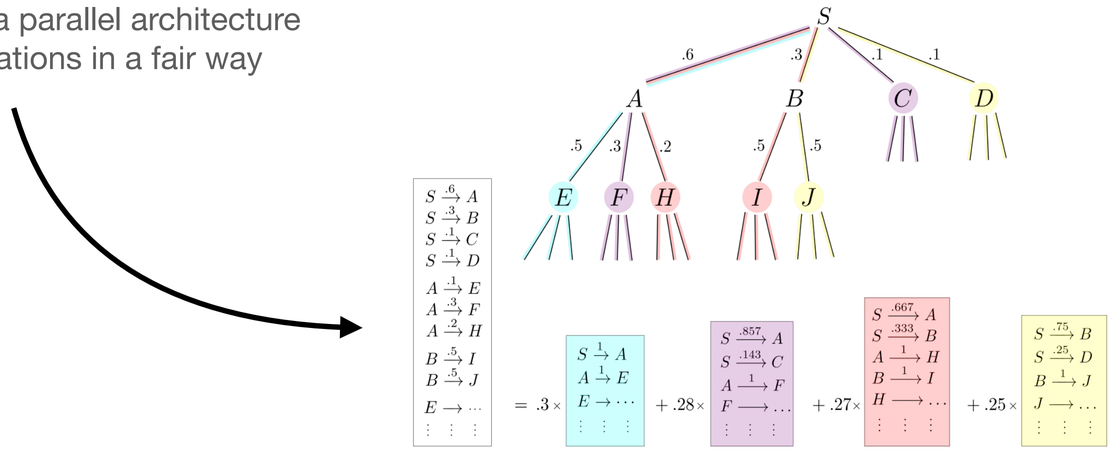

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How to sample? —> Construct a new PCFG for $\sqrt{D}$

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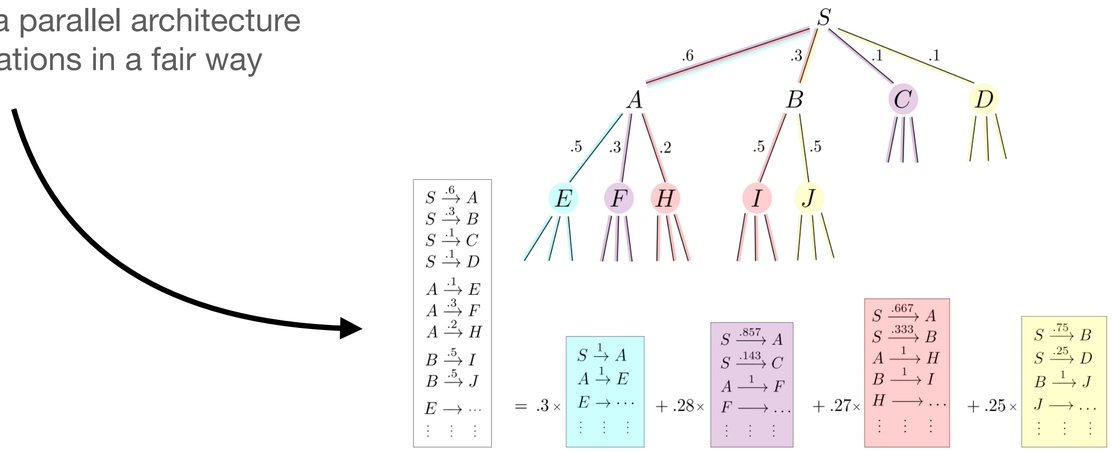

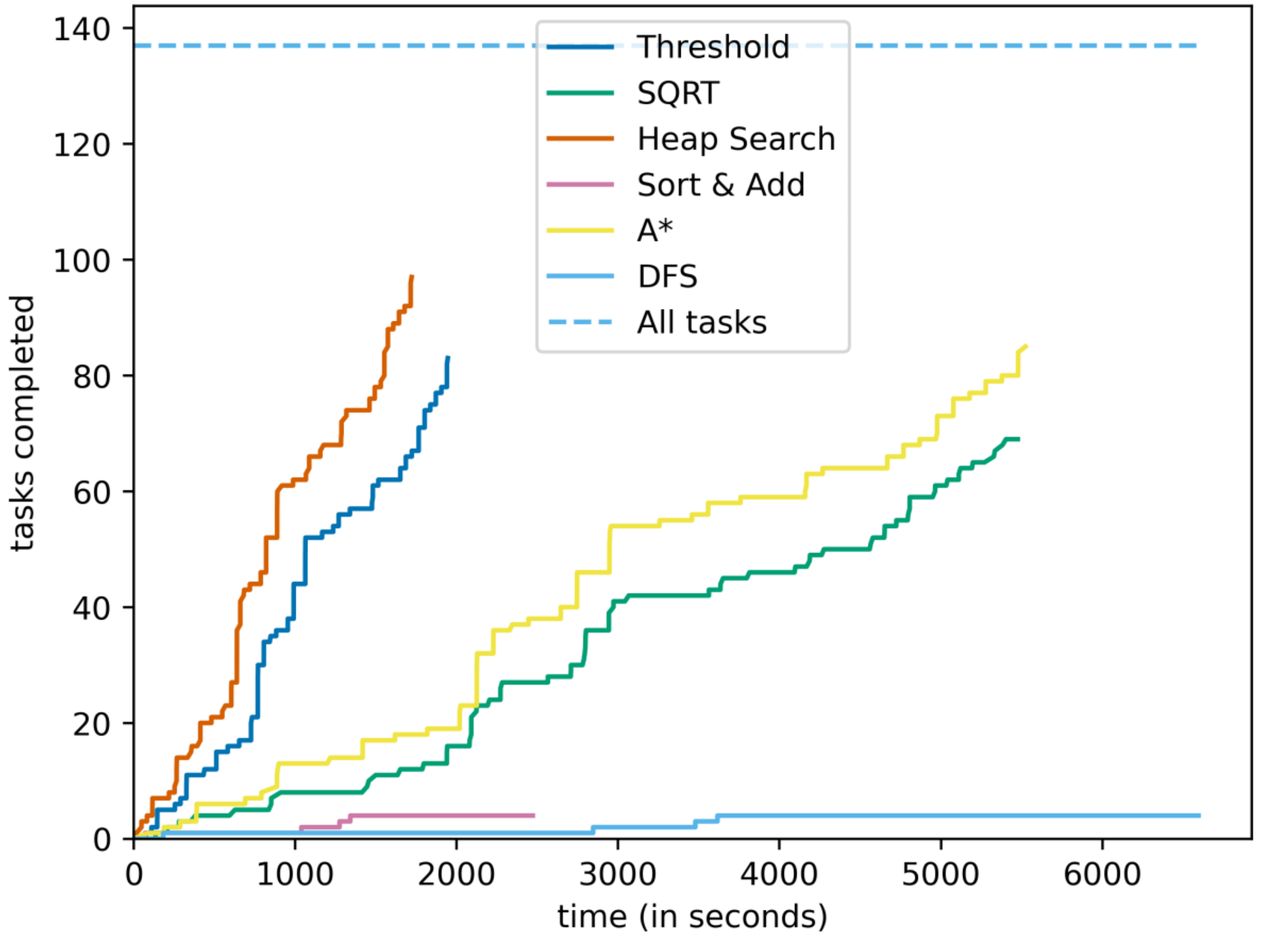

Figure 7: Comparing all search algorithms on the DreamCoder reduced dataset with machine-learned PCFGs

Thanks!

- Generic pipeline to do symbolic search on grammars enhanced with Machine Learning Predictions
- Check out **DeepSynth** (open-source tool) — https://deepsynth.labri.fr/
- Is heap search optimal (from an enumeration complexity POV)?
- Better sampling if using memory?
- Use feedback to refine the search?

Example

$$G\begin{cases} S \to \frac{1}{2} f(S,T) \mid \frac{1}{2} a \\ T \to b \end{cases}$$

Natural candidate:

$$G'\begin{cases} S \to \frac{1}{\sqrt{2}} f(S,T) \mid \frac{1}{\sqrt{2}} a \\ T \to b \end{cases}$$

G' indeed computes $\sqrt{\mathcal{D}}$ but it is not a PCFG, it needs renormalisation

for X non-terminal ($X = S, T$) define

$$[X] = \sum \{ \mathcal{D}(t) : t \text{ generated from } X \}$$

$$\begin{cases} [S] = \frac{1}{\sqrt{2}} [S][T] + \frac{1}{\sqrt{2}} \\ [T] = 1 \end{cases} \Rightarrow \begin{cases} [S] = 1 + \sqrt{2} \\ [T] = 1 \end{cases}$$

The PCFG computing $\sqrt{\mathcal{D}}$ is

$$\sqrt{G}\begin{cases} S \to \frac{1}{1+\sqrt{2}} \left(\frac{1}{\sqrt{2}} f(S,T) \mid \frac{1}{\sqrt{2}} a \right) \\ T \to b \end{cases}$$